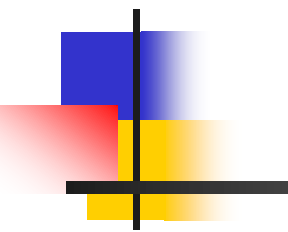


Spin effects in hadronic and heavy ion collisions: superstrong gravity probe?



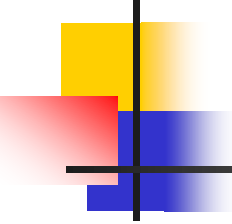
DSPIN2026

JINR, DUBNA, RUSSIA

Oleg Teryaev

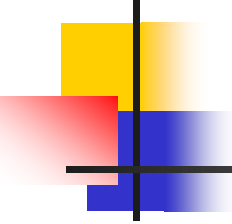
JINR

September 10, 2026



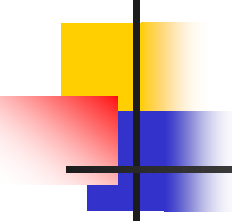
How strongest (QCD) and weakest (gravity) interactions are related?

- Hadronic matrix elements of energy-momentum tensor operator describe the interaction with classical gravity, and QCD hard exclusive processes
- The medium emerging in heavy-ion collisions manifests the highest ever acceleration and vorticity corresponding according to the Equivalence Principle to the superstrong "Equivalent" Gravity



Main Topics

- **E**quivalence **P**inciple: way to merge strongest and weakest interactions
- Gravitational Formfactors (“old” and “new”): **EP** for spin and its **Ex**tension
- Spin-1 in **exclusive** and **inclusive** processes: shear and **viscosity**
- Heavy ion collisions : highest vorticity and acceleration (=“equivalent” gravity)
- Anomalous current and polarization
- Unruh effect and temperature in medium



Electromagnetism vs Gravity (OT'99)

- Interaction – field vs metric deviation

$$M = \langle P' | J_q^\mu | P \rangle A_\mu(q)$$

$$M = \frac{1}{2} \sum_{q,G} \langle P' | T_{q,G}^{\mu\nu} | P \rangle h_{\mu\nu}(q)$$

- Static limit

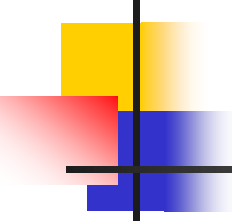
$$\langle P | J_q^\mu | P \rangle = 2e_q P^\mu$$

$$\sum_{q,G} \langle P | T_i^{\mu\nu} | P \rangle = 2P^\mu P^\nu$$
$$h_{00} = 2\phi(x)$$

$$M_0 = \langle P | J_q^\mu | P \rangle A_\mu = 2e_q M \phi(q)$$

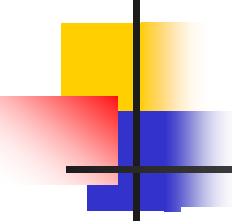
$$M_0 = \frac{1}{2} \sum_{q,G} \langle P | T_i^{\mu\nu} | P \rangle h_{\mu\nu} = 2M \cdot M \phi(q)$$

- Mass as charge – equivalence principle
- Low-energy theorem



EP and hadron structure

- “Microscopic” EP (coupling of gravity to EMT)
- +
- Conservation law
(Momentum SR to get local from LC pdf's):
 $\int dx x (\Sigma q(x) + G(x)) = 1$
- =
- “Macroscopic” EP (universal falling) :
- Tested VERY precisely



Gravitational Formfactors (Pagels'66, Ji'97, talks of K. Semenov-Tyan-Shanskiy, O. Selyugin): $O(\Delta)$

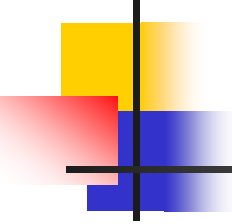
$$\langle p' | T_{q,g}^{\mu\nu} | p \rangle = \bar{u}(p') \left[A_{q,g}(\Delta^2) \gamma^{(\mu} p^{\nu)} + B_{q,g}(\Delta^2) P^{(\mu} i \sigma^{\nu)\alpha} \Delta_\alpha / 2M \right] u(p)$$

- Conservation laws - zero Anomalous Gravitomagnetic Moment : $\mu_G = J$ (g=2)

$$P_{q,g} = A_{q,g}(0) \quad A_q(0) + A_g(0) = 1$$

$$J_{q,g} = \frac{1}{2} [A_{q,g}(0) + B_{q,g}(0)] \quad A_q(0) + B_q(0) + A_g(0) + B_g(0) = 1$$

- No M_{pl} ! May be extracted from high-energy experiments/NPQCD calculations
- Describe the partition of angular momentum between quarks and gluons **Ji's SRs**
- **Describe interaction** with both **classical** and **"equivalent"** gravity



Gravitomagnetism

- Gravitomagnetic field (weak, except in gravity waves) – action on spin from $M = \frac{1}{2} \sum_{q,G} \langle P' | T_{q,G}^{\mu\nu} | P \rangle h_{\mu\nu}(q)$

$$\vec{H}_J = \frac{1}{2} \text{rot} \vec{g}; \quad \vec{g}_i \equiv g_{0i}$$

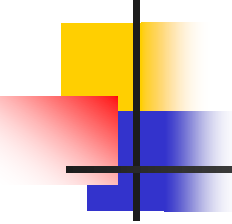
spin dragging twice
smaller than EM

- Lorentz force – similar to EM case: factor 1/2 cancelled with 2 from frequency same as EM

$$h_{00} = 2\phi(x) \quad \text{Larmor}$$

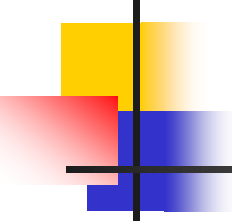
$$\omega_J = \frac{\mu_G}{J} H_J = \frac{H_L}{2} = \omega_L \quad \vec{H}_L = \text{rot} \vec{g}$$

- Orbital and Spin momenta dragging – the same - Equivalence principle
- Generalized for arbitrary strong fields
Obukhov, Silenko, OT, [1308.4552](#) and PRD



Equivalence principle

- Newtonian – “Falling elevator” – well known and checked (also for elementary particles)
- Post-Newtonian – gravity action on (**quantum!**) SPIN – known since 1962 (Kobzarev and Okun’; ZhETF paper contains acknowledgment to Landau: probably his last contribution to theoretical physics before car accident); rederived from conservation laws - Kobzarev and V.I. Zakharov
- Anomalous gravitomagnetic (and electric-CP-odd) moment is ZERO or
- Classical and QUANTUM rotators behave in the SAME way



Experimental test of PNEP

- Reinterpretation of the data on G(EDM) search

PHYSICAL REVIEW
LETTERS

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Search for a Coupling of the Earth's Gravitational Field to Nuclear Spins in Atomic Mercury

B. J. Venema, P. K. Majumder, S. K. Lamoreaux, B. R. Heckel, and E. N. Fortson

Physics Department, FM-15, University of Washington, Seattle, Washington 98195

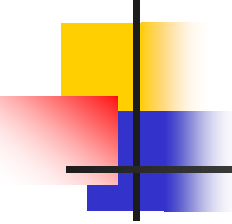
(Received 25 September 1991)

- If (CP-odd!) GEDM (new EMT FF, also forbidden by EP: extra γ_5 in B) = 0 $\rightarrow$ constraint for AGM (Silenko, OT'07) from Earth rotation – was considered as obvious (but it is just EP!) background

$$\mathcal{H} = -g\mu_N \mathbf{B} \cdot \mathbf{S} - \zeta \hbar \boldsymbol{\omega} \cdot \mathbf{S}, \quad \zeta = 1 + \chi$$

$$|\chi(^{201}\text{Hg}) + 0.369\chi(^{199}\text{Hg})| < 0.042 \quad (95\% \text{C.L.})$$

- Gravitational test of Ji's SR (for Hg)!
- New high precision EDM experiments: gravity is essential (NN Nikolaev, Vergeles, Obukhov, Silenko, OT, 2204.00427 and UFN)

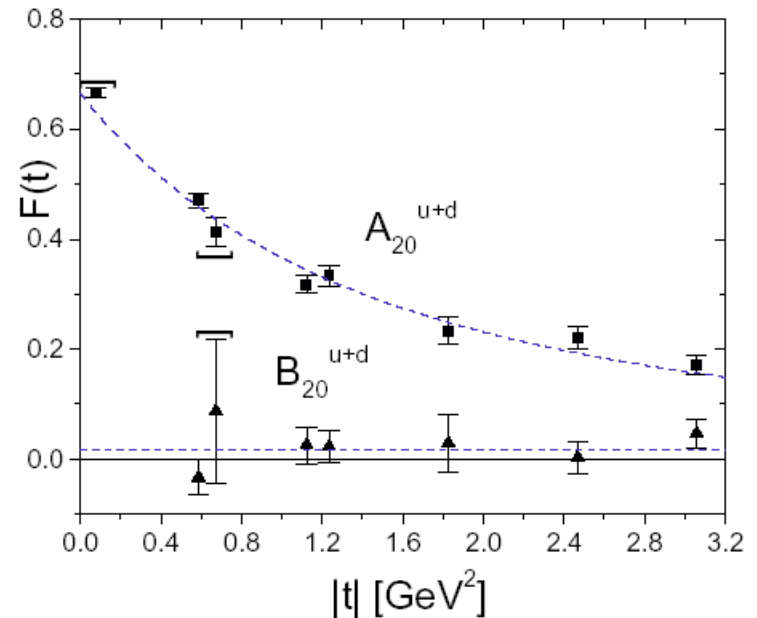
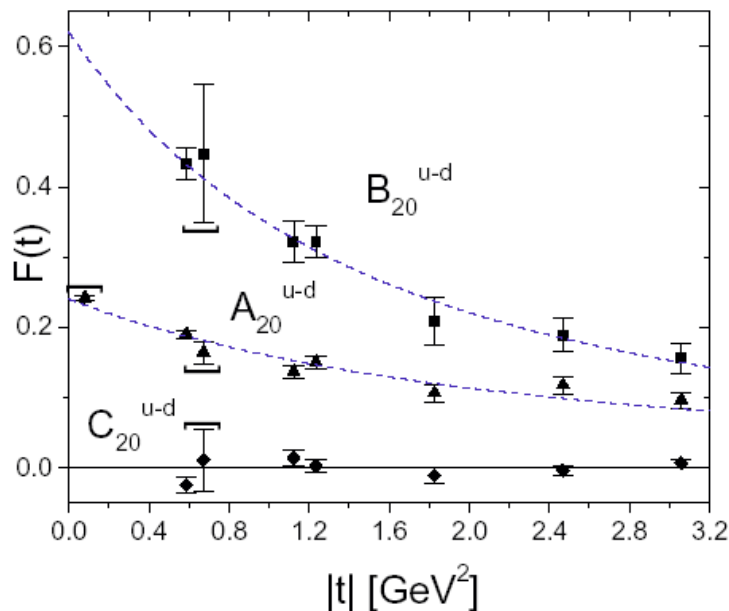


EP and quantum measurement

- If spin is just a geometric vector, EP for Earth's rotation is "trivial": looking from stars, spin rotates with Earth's angular velocity like Foucault pendulum
- Non-trivial if **quantum measurement** (quite **practical** here) is performed in the rotating frame
- Cf with Unruh effect (**measurement** in accelerated frame is crucial)

Extension of Equivalence principle

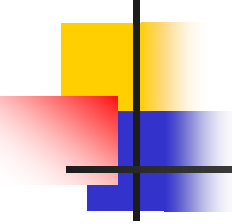
- Various arguments: $AGM \approx 0$ separately for quarks and gluons – most clear from the lattice (LHPC/SESAM)



Extended Equivalence

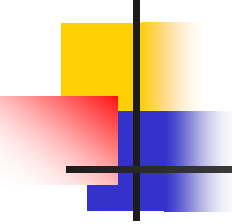
Principle=Exact EquiPartition

- In NLO pQCD – violated (LF:S.Brodsky et al.)
- Reason – in the case of ExEP- no smooth transition for zero fermion mass limit (Milton, 71)
- Conjecture (O.T., 2001 – prior to lattice data) – valid in NP QCD – zero quark mass limit is safe due to chiral symmetry breaking
- **Smallness of singlet AMM** (proton (1.79) and neutron (-1.91)) **is related to ExEP (OT'99)**: 1st and 2nd moments (with different parity: antiquarks subtracted for AMM and added for AGMM) of GPD $E(x, \xi)_{u+d}$
- **Gravityproof confinement**?! Nucleons are not broken even by black holes?!
- Equivalent gravity effect is absent (limited)?



Exact Equipartition and Pivot

- Important notion introduced by C. Lorce to relate transverse spin SR's of Ji&Yuan and Leader et al.
- Naïve interpretation of ExEP: common (approximately, averagely) pivot for quarks and gluons:
- $\langle J_{T(q,G)} \rangle = \langle x_0 \rangle \langle P_{L(q,G)} \rangle$
- Can this be satisfied for some of pivot choices?



Conformality (talk of A. Kataev) and ExEP

- Closeness of AMMs of proton (1.79) and neutron (-1.91) squared

$$\left. \frac{d\alpha_{g_1}(Q^2)}{dQ^2} \right|_{Q^2=0} = \frac{3\pi}{4g_A} \left(\frac{\kappa_n^2}{M_n^2} - \frac{\kappa_p^2}{M_p^2} \right)$$

- Relation between higher dimensional (in AdS QCD) and real gravity

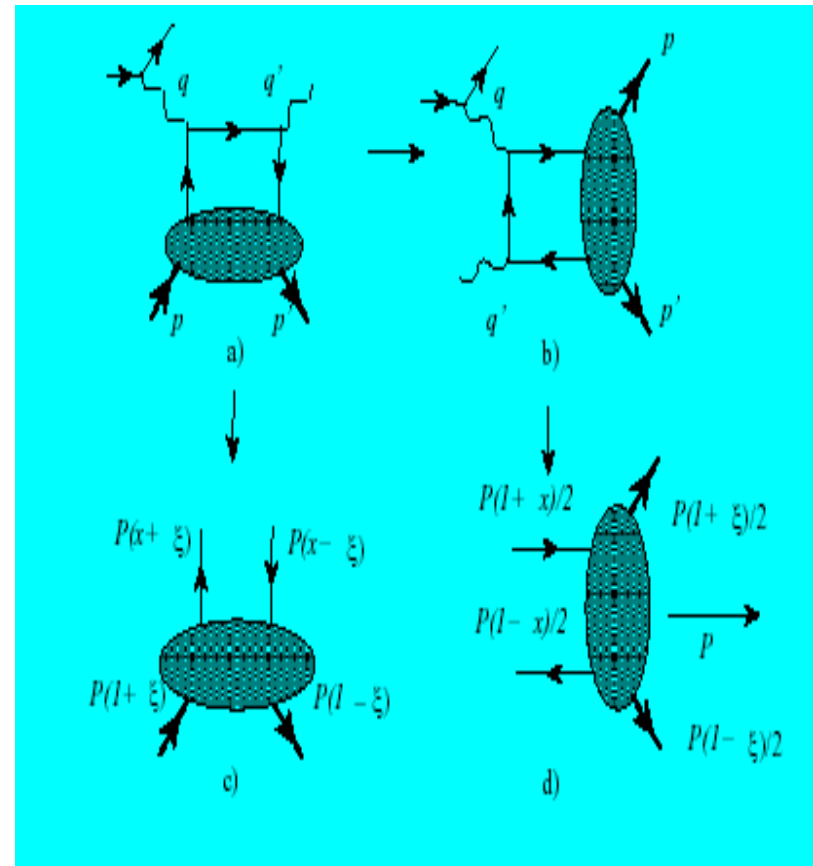
Also seen for $J=1$ if **density matrix** instead of wave functions is used for definitions of GPDs at $O(\Delta)$: $g=2$ is selected for EMT by conservation laws (OT'99)

SB Gerasimov was pointing out that in GDHSR for **arbitrary** spin AMM is counted as **$g-2$**

- $J=1/2 \rightarrow J=1$. QCD SR/model/**lattice (1608.03472; also K^* :2405.02600)** calculations of ρ -meson MM gives g close to 2 ($g=2$ exactly in AdS QCD). Why?
- **Maybe** because of similarity of moments and ExEP
- $g-2 = \langle E_u(x) \rangle$; $B = \langle x E_u(x) \rangle$
- Directly for ρ (because of isospin invariance combinations like $p+n$ for nucleons unnecessary!). Not reduced to non-extended EP: Gluons momentum fraction sizable
- Deutrons: also $g=2$ with good accuracy. Qualitative reason for ExEP. Quantitative – also may be done in AdS QCD containing already all necessary ingredients (talk of M. Allahverdiyeva)

Crossing for DVCS and GPD

- DVCS $\rightarrow$ hadron pair production in the collisions of real and virtual photons
- GPD $\rightarrow$ Generalized Distribution Amplitudes
- Duality between s and t channels
(Polyakov, Shuvaev, Guzey, Vanderhaeghen)



Gravitational FFs from Belle data on GDAs

S. Kumano, Qin-Tao Song and O. Teryaev, PRD 97 (2018) 014020.

- Gravitational FFs are related to twist-2 GDAs

$$A_{\lambda_1 \lambda_2} = T_{\mu\nu} \varepsilon^\mu(\lambda_1) \varepsilon^\nu(\lambda_2) / e^2$$

$$A_{++} = \sum_q \frac{e_q^2}{2} \int_0^1 dz \frac{2z-1}{z(1-z)} \Phi^q(z, \xi, W^2)$$

$$\int dz (2z-1) \Phi_q^+(z, \xi, W^2) = \frac{2}{(P^+)^2} \langle \pi^+(p_1) \pi^-(p_2) | T_q^{++}(0) | 0 \rangle$$

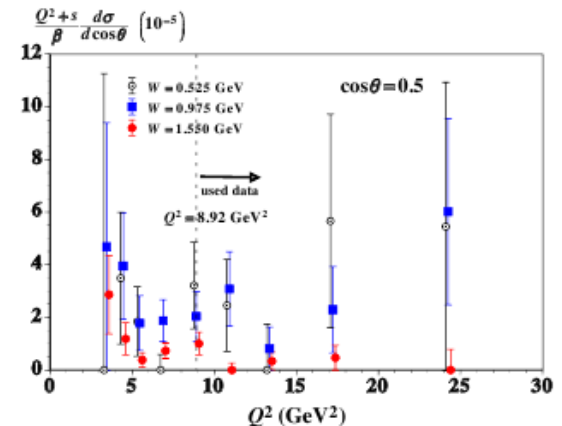
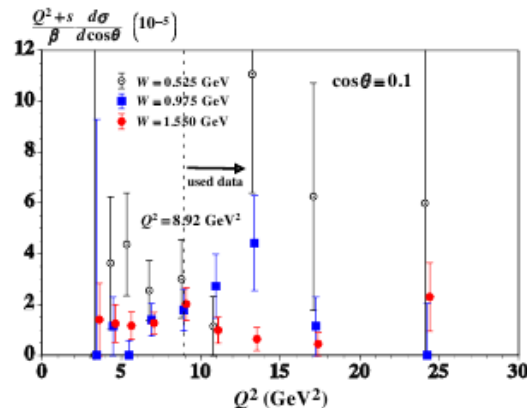
$$\langle \pi^0(p_1) \pi^0(p_2) | T^{\mu\nu}(0) | 0 \rangle = \frac{1}{2} \left[(s g^{\mu\nu} - P^\mu P^\nu) \Theta_1 + \Delta^\mu \Delta^\nu \Theta_2 \right]$$

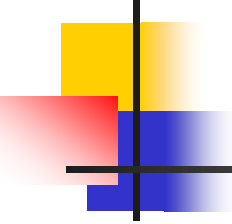
M. Masuda et al. [Belle Collaboration], PRD 93 (2016), 032003

$$P = p_1 + p_2, \Delta = p_1 - p_2$$

- Belle data and scaling : $W=0.525, 0.975, 1.55$ GeV

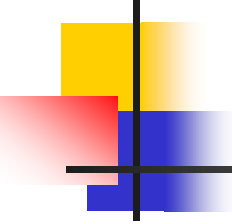
$$\frac{(Q^2+s)d\sigma}{\beta d|\cos\theta|} \propto |\Phi^{s^0 s^0}(z, \cos\theta, W, Q)|^2$$





New EMT formfactor : Shear viscosity

- From spherically symmetric object to fluid (EoS!)
- $T^{\mu\lambda} = (e+p) v^\mu v^\lambda - p g^{\mu\lambda}$
- $V^\mu = P^\mu/M$: correct normalization but no coordinate dependence
- Another suggestion (OT'19):
- $V^\mu = (P^\mu + a(t) k_T^\mu) / (M^2 + a^2(t) k_T^2)^{1/2}$
- Viscosity: $\eta dv^\mu/dx_T^\lambda \sim E_\eta p^{[\mu} \Delta^{\lambda]}$
- NO such term in total EMT (but can be for quarks separately)
- Naïve T-oddness: phases in GPD channel from decays in TGPDs (talk of K. Semenov-Tyan-Shanskiy)
- Phases $\leftrightarrow$ dissipation: polarization in pionic superfluidity model (V. I. Zakharov, OT' 17)

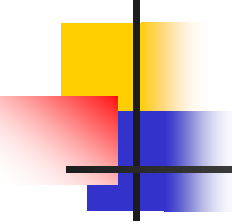


Viscosity in GDA channel

- Viscosity: will correspond to **Exotic $J^{PC}=1^{-+}$** meson (studied long ago without mentioning gravity: Anikin, Pire, Szymanowski, OT, Wallon'06)
- Spin: related to structure of matrix element: One index of EMT (0^{th} in rest frame) is carried by momentum and other by polarization vector - just what we need for **viscosity**
- **NO for conserved EM: zero coupling for (G)DA!**
- **$\pi\eta$** pairs observation instead of $\pi\pi$ required : related by crossing to transition GPDs(talk of K. Semenov-Tyan-Shanskiy)
- Smallness of viscosity: related to smallness of exotic GDAs and ExEP violation?!
- Calculation in perturbative limit: Song, OT, Yoshida (2503.11316 and PLB): relation to meson's DA

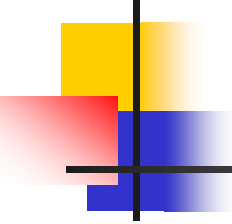
Viscosity for GDAs and holography

- Terms in EMT:
- $(e+p) v^\mu v^\lambda \sim A P^\mu P^\lambda$
- $\eta dv^\mu/dx_T^\lambda \sim E_\eta p^{[\mu} \Delta^{\lambda]}$
- TD: $e+p \rightarrow Ts$
- $\eta/s (> 1/(4\pi)) \sim E_\eta T / AM$
- Correct dependence on Planck constant recovered via $\Delta^\lambda \rightarrow -i\hbar d/dx_T^\lambda$



Spin 1 EMT and **inclusive** processes

- Forward matrix element $\rightarrow$ density matrix
- Contains **P-even** term: tensor polarization $S^{\alpha\beta}$
New EMT FF
- $\langle P | T^{\alpha\beta} | P \rangle = A P^\alpha P^\beta + T S^{\alpha\beta}$
- Symmetric and **traceless**: correspond to (average) **shear** forces
- Cf with spin $1/2$ and spin 1 vector polarization : **P-odd** vector polarization requires another vector (q) to form vector product



SUM RULEs

- Efremov, OT'82 : zero sum rules:
- Current conservation: 1st moment: also in parton model by Close and Kumano (90)
- EMT conservation: 2nd moment (forward analog of Ji's SR: $\sum B=0 \Leftrightarrow \sum T=0$)
- Average shear force (compensated between quarks and gluons)
- Gravity and (Ex)EP (zero average shear separately for quarks and gluons) – OT'09
- EP: No monopole spin-gravity coupling!
- Deutrons in $|0\rangle$ and $(|1\rangle + |-1\rangle)/\sqrt{2}$ states fall in the same way
- C.f. with Protons and electrons: $|1/2\rangle$ and $|-1/2\rangle$ -----//-----

Manifestation of post-Newtonian (Ex)EP for spin 1 hadrons

- Tensor polarization - coupling of EMT to spin in forward matrix elements - inclusive processes
- Second moments of tensor distributions should sum to zero

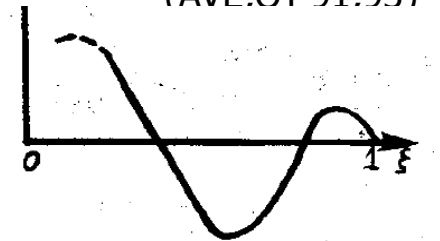
$$A_T = \frac{\sigma_+ + \sigma_- - 2\sigma_0}{3\bar{\sigma}}$$

$$\int_0^1 C_i^T(x) dx = 0$$

$$\langle P, S | \bar{\psi}(0) \gamma^\nu D^{\nu_1} \dots D^{\nu_n} \psi(0) | P, S \rangle_{\mu^2} = i^{-n} M^2 S^{\nu\nu_1} P^{\nu_2} \dots P^{\nu_n} \int_0^1 C_q^T(x) x^n dx \quad (\text{AVE.OT'91.93})$$

$$\sum_q \langle P, S | T_i^{\mu\nu} | P, S \rangle_{\mu^2} = 2P^\mu P^\nu (1 - \delta(\mu^2)) + 2M^2 S^{\mu\nu} \delta_1(\mu^2)$$

$$\langle P, S | T_g^{\mu\nu} | P, S \rangle_{\mu^2} = 2P^\mu P^\nu \delta(\mu^2) - 2M^2 S^{\mu\nu} \delta_1(\mu^2)$$

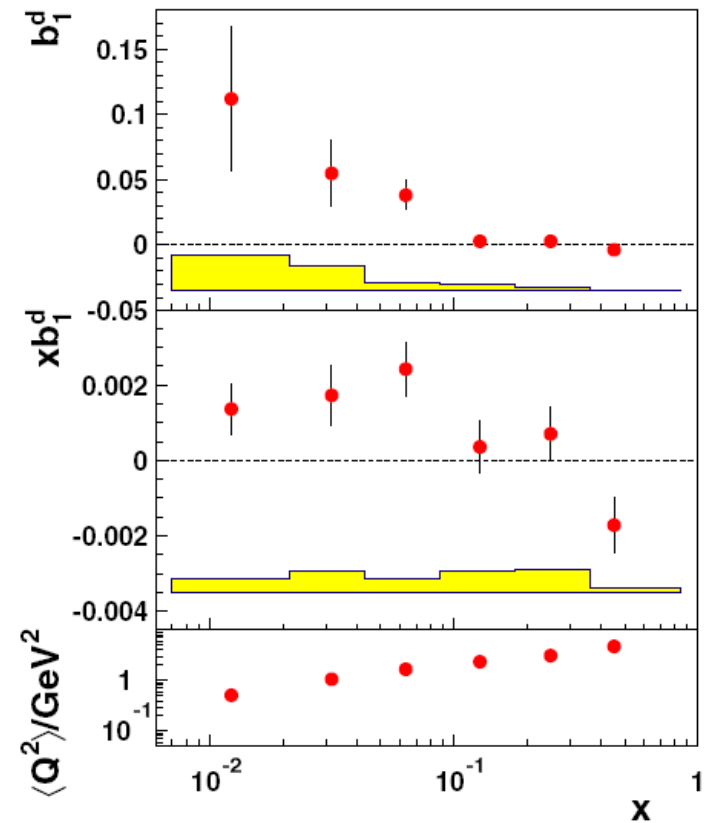


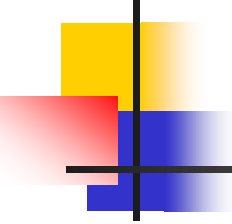
$$\sum_q \int_0^1 C_i^T(x) x dx = \delta_1(\mu^2) = 0 \quad \text{for ExEP}$$

HERMES – data on tensor spin structure function

PRL 95, 242001 (2005)

- Isoscalar target – proportional to the sum of u and d quarks – combination required by (Ex)EP
- Second moments – compatible to zero better than the first one (collective tensor polarized glue << sea)

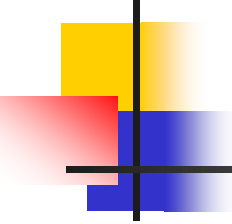




Where else to test?

- EIC?
- DY@J-PARC: (Song,Kumano:1902.04712)
- ET'82-**any** hard process
- $f_{A1} \sim b_1$

$$\frac{P_{xx} - 2P_{yy} - 2P_{zz}}{3 \int_0^1 d\xi f(\xi) \text{Sp}[\hat{P} E(\xi, P)]} = \frac{2F_{A1}(x_1^*, x_2^*)}{3F(x_1, x_2)}$$
- Suggestion: **hadronic** (pion) inclusive tensor SSA(OT'19)
- $A = (d\sigma(1)+d\sigma(-1)-2 d\sigma(0))/(d\sigma(1)+d\sigma(-1)+d\sigma(0))$
- Complementary to other deuteron studies at SPD (talk of N. Nikolaev)

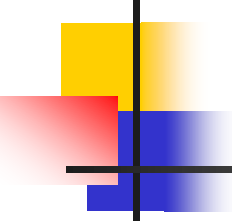


EP: Where is the fastest possible rotation and acceleration?

- Non-central heavy ion collisions (Angular velocity $\sim c/\text{Compton wavelength}$) $\Omega \sim \frac{c}{\lambda_p} = \frac{m_p c^2}{\hbar}$
- ~ 25 orders of magnitude faster than Earth's rotation $\eta_{\text{rot}} = \frac{\Omega}{\omega_{\oplus}} = \frac{c}{R_A} \cdot \frac{T_{\oplus}}{2\pi} = \frac{1}{2\pi} \cdot \frac{cT_{\oplus}}{R_A} \approx 10^{27}$
- Differential rotation – vorticity
- P-odd : May lead to various P-odd effects (Chiral magnetic/vortical effects)
- Acceleration: even larger ratio with the gravity of Earth

$$\eta_{\text{acc}} = \frac{c}{R_A} \cdot \frac{c}{g_{\oplus}} = \eta_{\text{rot}} \frac{2\pi c}{T_{\oplus} g_{\oplus}} \approx 10^{30}$$

$$\eta_{\text{acc}} = \frac{c}{R_A} \cdot \frac{c}{g_{\oplus}} = \frac{c^2}{v_{\oplus}^2} \cdot \frac{R_{\oplus}}{R_A}$$



HIC: Strong interactions and superstrong “EP-gravity”
(explored in lattice simulations: talks of V. Zakharov,
Yu. Obukhov, V. Braguta, A. Roenko, J. Day,
V. Voronyuk, N. Tsegelnik, E. Dlin)

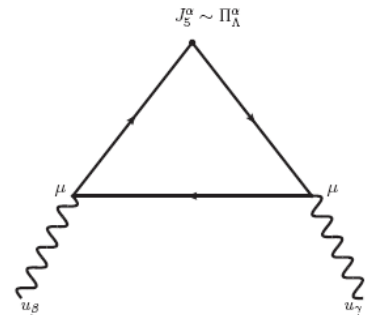
- $E_{EM}/E_G \sim e^2/(m/M_{Pl})^2$ $M_{Pl} \sim 10^{18} \text{ GeV}$
- For 2 particles with M_{Pl} mass at Compton wavelength distance ($1/M_{Pl}$): $E_G \sim (G = 1/M_{Pl}^2) M_{Pl}^2 / (1/M_{Pl}) = M_{Pl}$
 $g \sim (G = 1/M_{Pl}^2) M_{Pl} / (1/M_{Pl})^2 = M_{Pl}$
- Gravitational interaction is **strongly** suppressed wrt strong one $\sim (\Lambda/M_{Pl})^2$
- **Equivalence Principle**
- **I: Acceleration $\leftrightarrow$ Gravity**
- HIC: $a \sim \Lambda$, $a/g \sim \frac{c^2}{v_\oplus^2} \cdot \frac{R_\oplus}{R_A} \sim 10^{30}$
- $M_{Pl} \rightarrow \Lambda$ (“GeV Gravity” to be compared with ‘TeV gravity’ from extra dimensions)

Effective field theory: Anomalies

- 4-Velocity is also a **GAUGE FIELD** (V.I. Zakharov et al)

$$e_j A_\alpha J^\alpha \Rightarrow \mu_j V_\alpha J^\alpha$$

- Triangle anomaly leads to polarization of quarks and hyperons (Rogachevsky, Sorin, OT '10)
- Analogous to anomalous gluon contribution to nucleon spin (Efremov, OT'88)
- 4-velocity instead of gluon field potential and vorticity -----//-----
(chromo)magnetic field strength!



*Observable for AVE: polarization (talks of
A. Taranenko, A. Jaiswal, A. Ayala, E.
Alpatov, V. Troshin, S. Rode, V/ Voronyuk,
N. Tsegelnik, J.J. Medina Serna)*

O. Rogachevsky, A. Sorin, O. Teryaev
Chiral vortical effect and neutron asymmetries in
heavy-ion collisions
PHYSICAL REVIEW C 82, 054910 (2010)

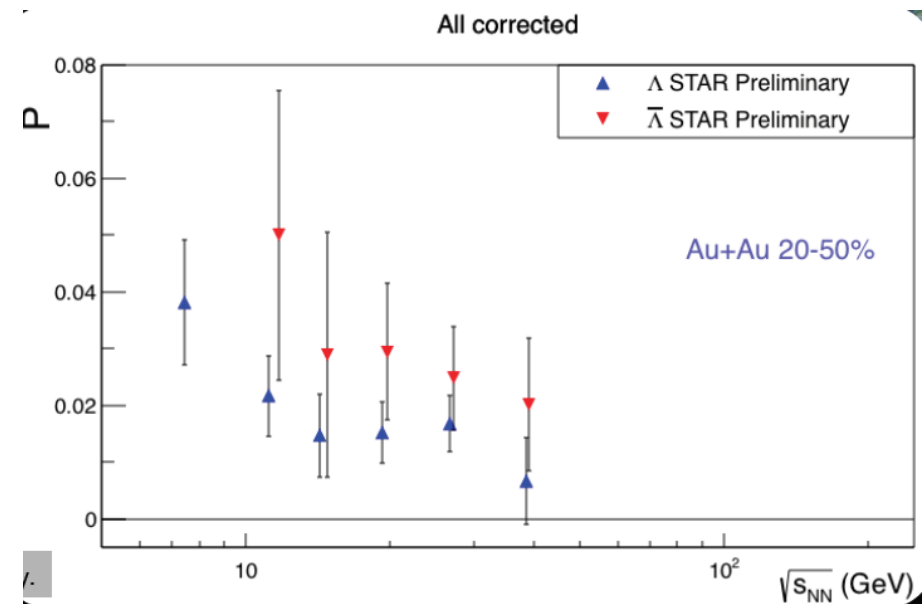
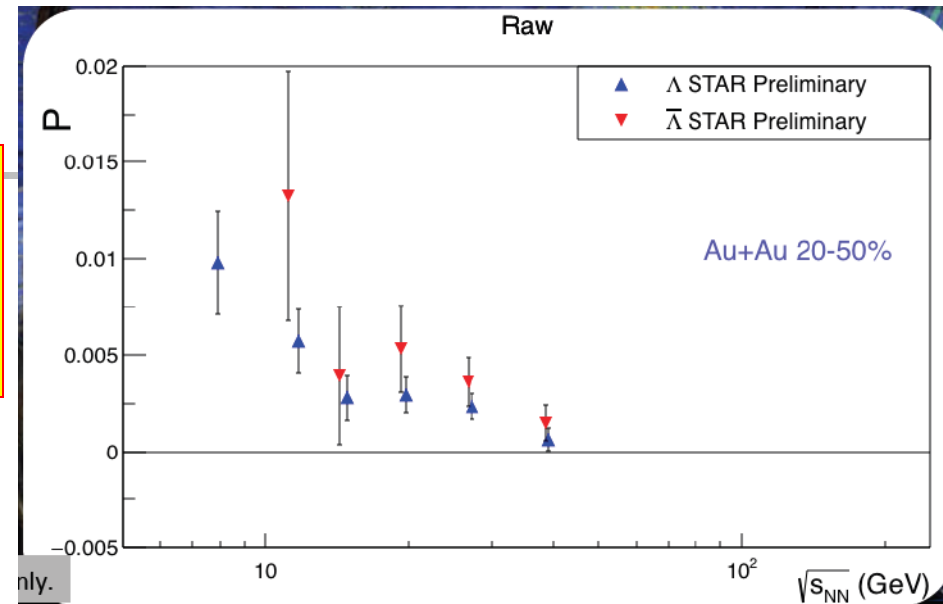
One would expect that polarization is proportional to the anomalously induced axial current [7]

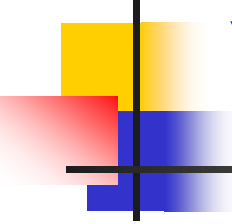
$$j_A^\mu \sim \mu^2 \left(1 - \frac{2\mu n}{3(\epsilon + P)} \right) \epsilon^{\mu\nu\lambda\rho} V_\nu \partial_\lambda V_\rho, \quad (6)$$

where n and ϵ are the corresponding charge and energy densities and P is the pressure. Therefore, the μ dependence of polarization must be stronger than that of the CVE, leading to the effect's increasing rapidly with decreasing energy.

This option may be explored in the framework of the program of polarization studies at the NICA [17] performed at collision points as well as within the low-energy scan program at the RHIC.

STAR, Nature 548 (2017) 62-65





“Anomalous” mechanism

- **P**rediction of decrease with energy (due to chemical potential)
- **P**rediction of $P \sim 1\%$

BAZNAT, GUDIMA, SORIN, AND TERYAEV

$$\langle P_\Lambda \rangle \sim \frac{\langle \mu^2 \rangle N_c H}{2\pi^2 \langle N_\Lambda \rangle}$$

PHYSICAL REVIEW C **88**, 061901(R) (2013)

For numerical estimate at NICA energies, we take (see Fig. 3) $H = 30 \text{ fm}^2 (c = 1)$ and, as typical values, $\langle \mu^2 \rangle = 900 \text{ MeV}^2$, $\langle N_\Lambda \rangle = 15$ to get $\langle P_\Lambda \rangle \sim 0.8\%$. This value is

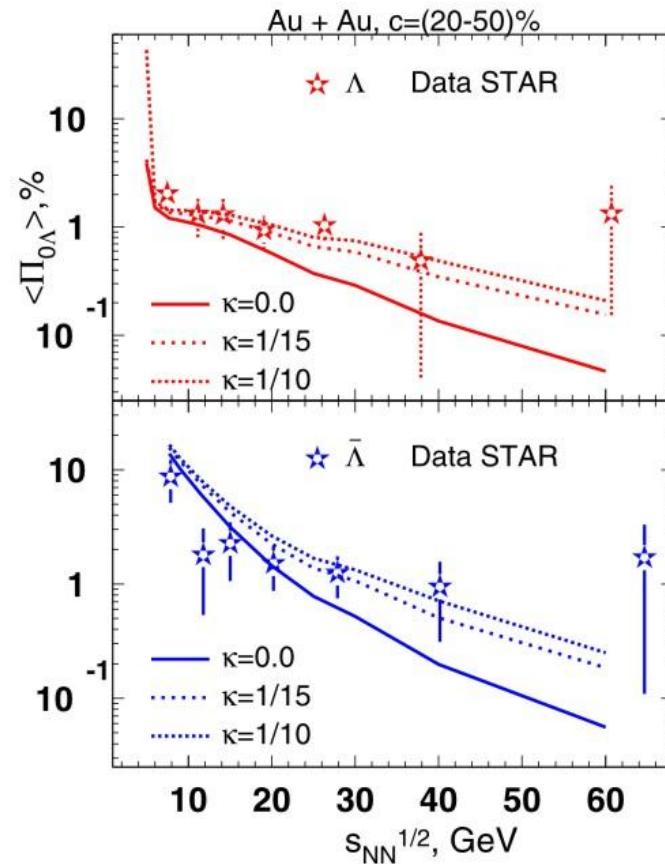
- **P**ostdiction of larger polarization of antilambdas

ALEXANDER SORIN AND OLEG TERYAEV

PHYSICAL REVIEW C **95**, 011902(R) (2017)

The proportionality of the polarization to the square of the chemical potential related to C -even parity of axial current leads to the same sign of polarization of Λ and $\bar{\Lambda}$ hyperons. The smaller number of the latter should result in a larger fraction of the axial charge, corresponding to each antihyperon and to a larger absolute value of polarization. Detailed numerical sim-

Λ vs Anti Λ : *same* axial charge is distributed between *lower* number of hadrons (*also* for Ω^- - ?!)



TD approach to gauge anomaly (D.T. Son and P. Surowka; S.-Z. Yang, J.-H. Gao and Z.-T. Liang) -> gravitational anomaly

Gravitational chiral anomaly in hydrodynamics

G. Yu. Prokhorov, O.V. Teryaev, V.I. Zakharov, Phys. Rev. Lett. 129, 151601 (2022)

- In heavy ion collisions (in particular, at **NICA**) a relativistic quantum liquid is formed with **extremely high vorticity** ω^μ and **acceleration** a^ν . The axial current is related to the hyperon **polarization**. **New** contributions to current and **polarization**:

KVE:

$$j_A^\mu = \lambda_1(\omega_\nu \omega^\nu) \omega^\mu + \lambda_2(a_\nu a^\nu) \omega^\mu$$

Transport coefficients

- The novel kinematical vortical effect (KVE)** depends only on vorticity and acceleration, but is independent of **temperature** and **chemical potential**, and is determined by a **quantum anomaly** in **curved** space.
- The effect exists even when there are **no gravitational** fields ('Cheshire cat' or 'Structural stability of hydrodynamics')
- Derivation is essentially making use of the method developed (for the case of electromagnetic fields) In the paper
- Besides further exploration of the anomalous transport the collaboration in investigations of various **polarization effects** in hadronic and heavy-ion collisions would be of great importance for us. Both the theoretical studies and modeling for experiments (in particular, at **NICA and HIAF**) are of interest

Connection with anomaly and gravity:

$$\lambda_1 - \lambda_2 = 32\mathcal{N}$$

$$\nabla_\mu j_A^\mu = \mathcal{N} \epsilon^{\mu\nu\alpha\beta} R_{\mu\nu\lambda\rho} R_{\alpha\beta}{}^{\lambda\rho}$$

[27] Shi-Zheng Yang, Jian-Hua Gao, and Zuo-Tang Liang, Constraining non-dissipative transport coefficients in global equilibrium, *Symmetry* **14**, 948 (2022).



Statistics vs geometry: Unruh effect (Becattini'18; Prokhorov, OT, Zakharov'19)

- Results for energy density of thermal system in **Minkowski** space coincide with the early known for the space with conical singularity (e.g. cosmic strings)

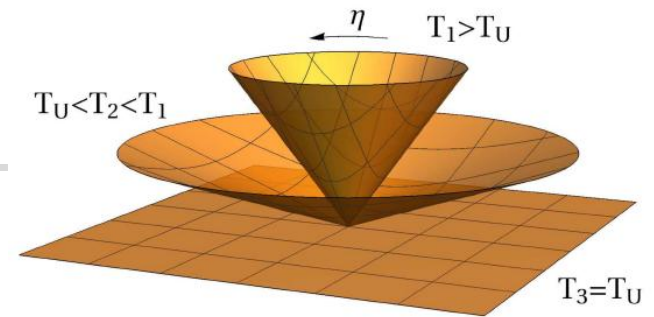
$$c_V = \frac{\mu_s^2 + \mu_A^2}{2\pi^2} + \frac{T^2}{6}, \quad Q_5^s = N_c \int d^3x c_V \gamma^2 \epsilon^{ijk} v_i \partial_j v_k$$

$$\rho_{s=0} = \frac{\pi^2 T^4}{30} + \frac{T^2 |a|^2}{12} - \frac{11 |a|^4}{480 \pi^2},$$

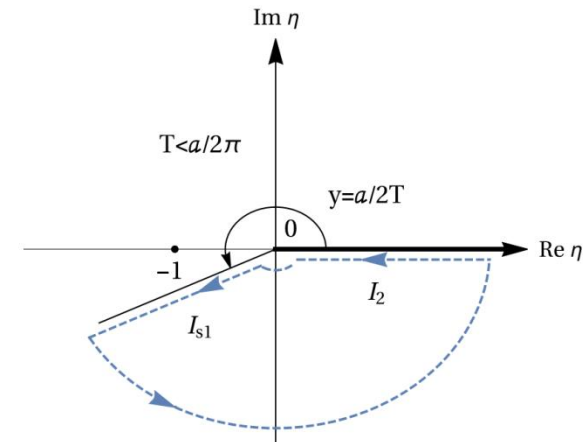
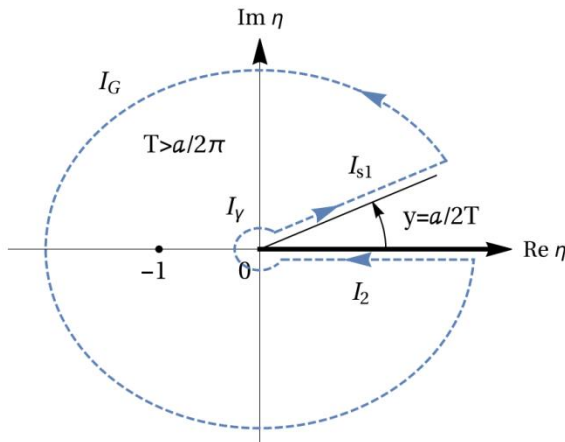
$$\rho_{s=1/2} = \frac{7\pi^2 T^4}{60} + \frac{T^2 |a|^2}{24} - \frac{17 |a|^4}{960 \pi^2}$$

- Energy density turns to zero for $T=T_U=a/(2\pi)$ (~"physical conditions of renormalization". also simple explanation of coefficient)
- Unruh effect explains **fast** HIC thermalization

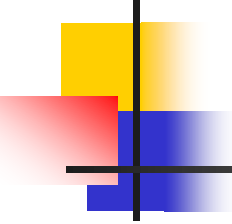
Instability for high accelerations



- Normally $T > T_U$
- Fast acceleration without thermalization: instability (leads to **hadronization**)



- EP $\sim$ fall to BH?



Hawking vs Unruh effects

- Pair creation in gravity field or accelerated frame
- EP: $g=a: \Rightarrow T_H=T_U$
- One particle goes to observer outside BH or accelerating detector
- Second particle falls to the BH or goes to inertial observer
- Observation of thermal spectra in HIC $\sim$ looking from BH interior

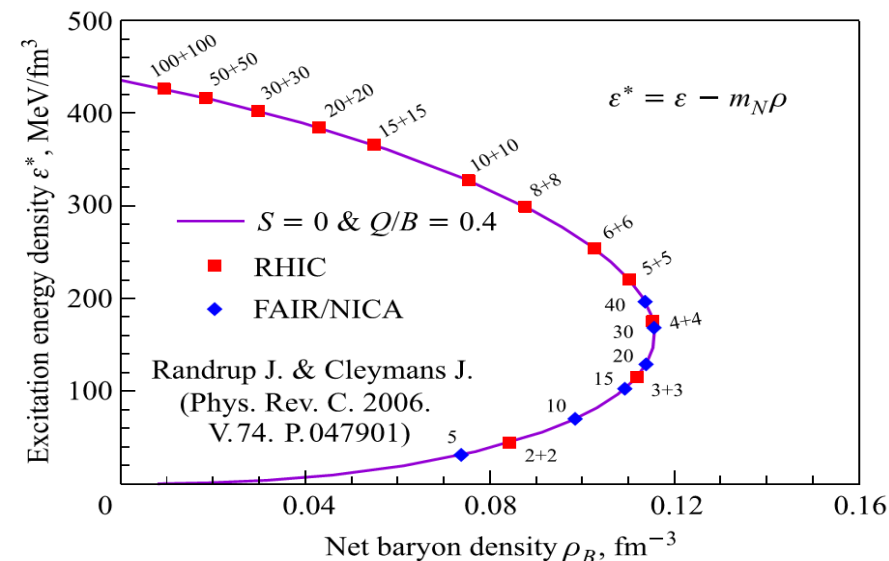
NICA (**N**uclotron based **I**on **C**ollider **f**acility)

– the flagship project in HEP
of Joint Institute for Nuclear Research (JINR)

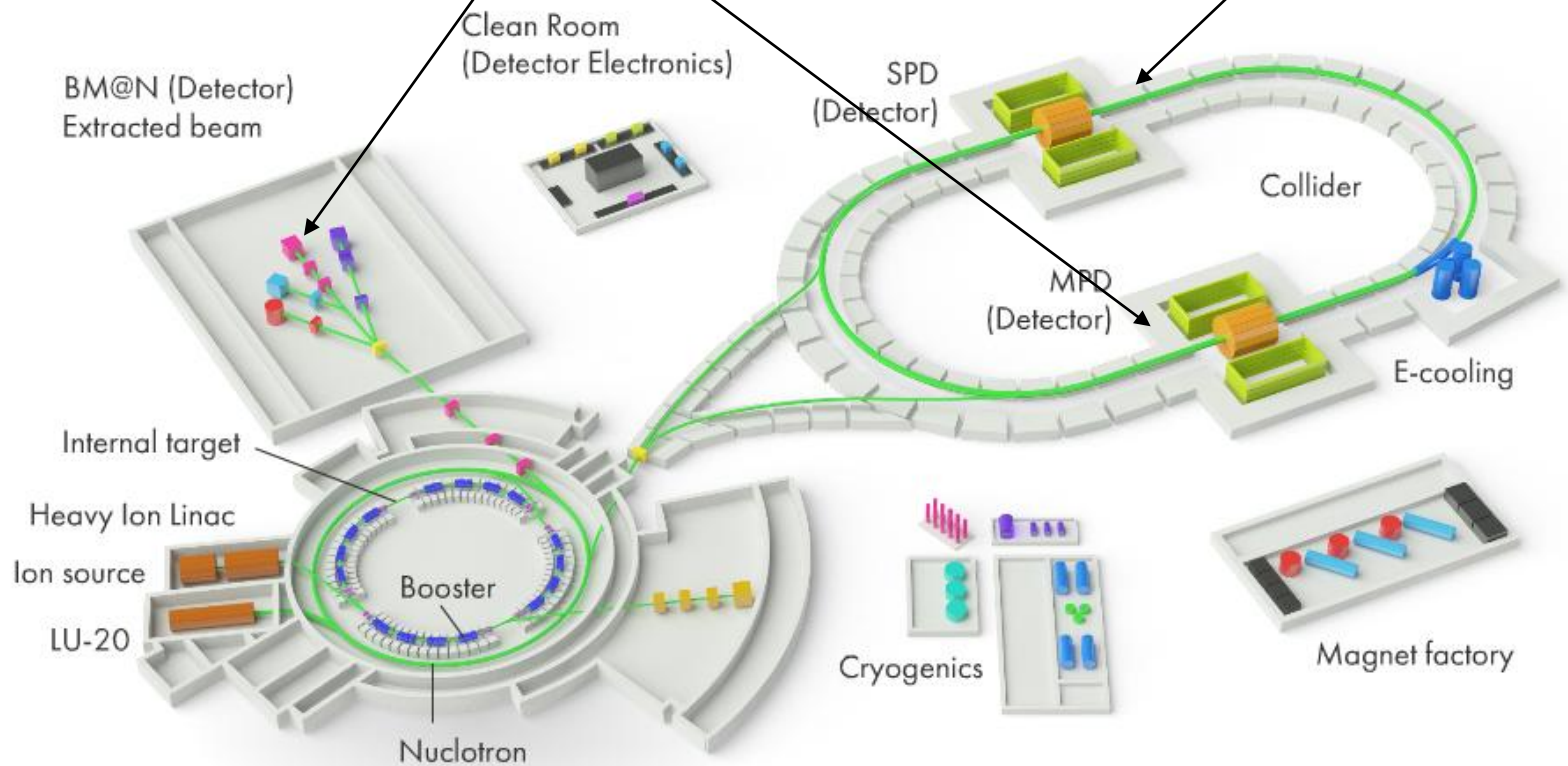
Main targets of “NICA Complex”:

- **study of hot and dense baryonic matter**
- investigation of hadronic spin structure through various polarization phenomena
- development of accelerator facility for HEP @ JINR providing intensive beams of relativistic ions from p to Au

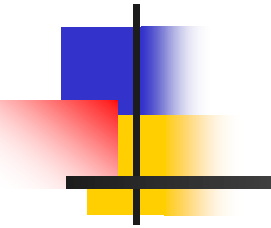
polarized protons and deuterons
with energy up to
 $\sqrt{s}_{NN} = 11 \text{ GeV}$ (Au^{79+} , $L \sim 10^{32} \text{ cm}^{-2} \text{ c}^{-1}$)
 $\sqrt{s} = 27 \text{ GeV}$ (p , $L \sim 10^{32} \text{ cm}^{-2} \text{ c}^{-1}$)

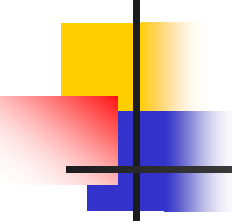


NICA: heavy ions and hadrons



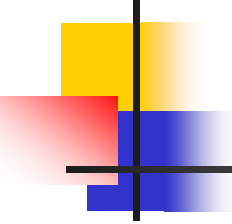






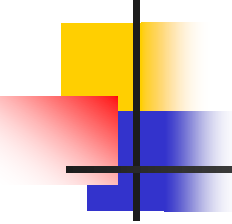
CONCLUSIONS

- Interplay of QCD and gravity in hadronic and heavy-ion collisions
- Special role of fundamental notions of Equivalence Principle and Quantum Measurement
- Special role of tensor and global polarization
- Modern accelerators (LHC, RHIC, CEBAF EIC, EIC, FAIR, NICA, HIAF... also “equivalent gravity” labs (with “access” to BH interior☺))

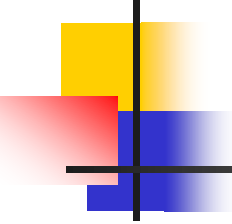


Outlook: hadronic and HIC interplay in both directions

- Hadronic medium properties (viscosity) from GrFFs
- Coupling of in-medium hadrons to acceleration and vorticity via GrFFs
- ?



BACKUP



Equivalence principle for moving particles EP^{II} vs EP^I

- Compare gravity and acceleration: gravity provides EXTRA space components of metrics
- Matrix elements DIFFER $h_{zz} = h_{xx} = h_{yy} = h_{00}$
$$\mathcal{M}_g = (\epsilon^2 + p^2)h_{00}(q), \quad \mathcal{M}_a = \epsilon^2 h_{00}(q)$$
- Ratio of accelerations: $R = \frac{\epsilon^2 + p^2}{\epsilon^2}$ - confirmed by explicit solution of Dirac equation (Silenko, OT, '05)
- Arbitrary fields – Obukhov, Silenko, OT '09, '11, '13, 16, 17: also the same dynamics for classical and quantum rotators (“EP for strong fields”)

Gravity vs accelerated frame for spin and helicity

- Spin precession – well known factor 3 (Probe B; spin at satellite – probe of PNEP!) – smallness of relativistic correction ($\sim \mathbf{P}^2$) is compensated by $1/\mathbf{P}^2$ in the momentum direction precession frequency
- Helicity flip – the same!
- No helicity flip in gravitomagnetic field – another formulation of PNEP (OT'99) and
- Flip by “gravitoelectric” field: relic neutrino (Anisotropic Universe: Kamenshchik, OT'15)? Black hole?

$$\frac{d\sigma_{+-}}{d\sigma_{++}} = \frac{tg^2(\frac{\phi}{2})}{(2\gamma - \gamma^{-1})^2}$$

Cosmological implications of PNEP

- Necessary condition for Mach's Principle (in the spirit of **S.Weinberg's** textbook-Section 9.7)
- Lense-Thirring inside massive rotating empty shell (=model of Universe)
- For **flat** "Universe" - precession frequency equal to that of shell rotation
- Simple observation-Must be the same for classical and **quantum** rotators – PNEP!
- More elaborate models - Tests for cosmology ?!

